## Lesson Two

## Quadratic Functions Expansions and Compressions

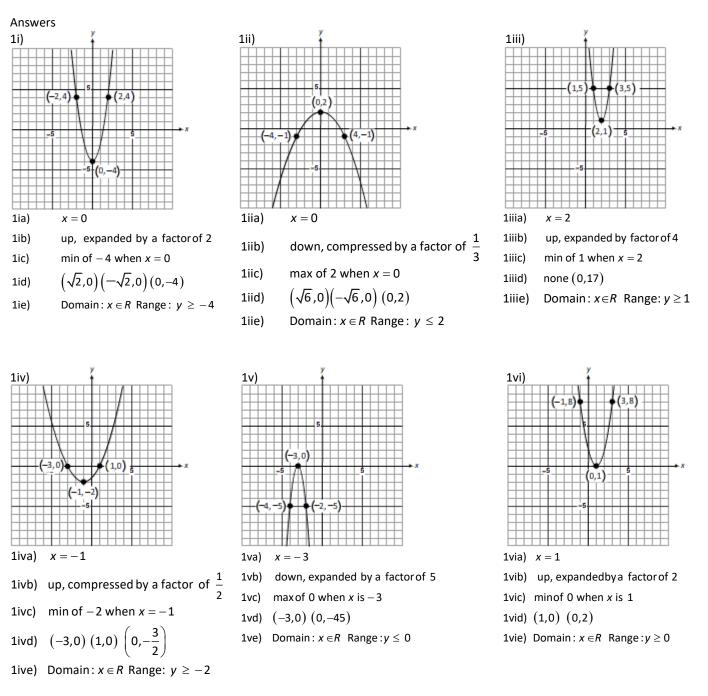
- 1. Sketch the graph for each of the following without a calculator (label vertex and the coordinates of two other points) and then state:
  - a) equation of axis of symmetry
  - b) direction of opening and by what factor the graph has been expanded of compressed vertically
  - c) the maximum or minimum value
  - d) exact values of the x-intercept(s) (if any) and the y-intercept
  - e) the domain and range

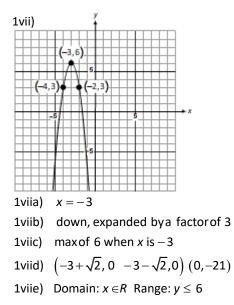
i) 
$$y = 2x^2 - 4$$
  
ii)  $y = -\frac{1}{3}x^2 + 2$   
iii)  $y = 4(x - 2)^2 + 1$   
iv)  $y = \frac{1}{2}(x + 1)^2 - 2$   
v)  $y = -5(x + 3)^2$   
vi)  $y = 2(x - 1)^2$   
vii)  $y = -3(x + 3)^2 + 6$   
viii)  $y = -(x - 1)^2 - 3$ 

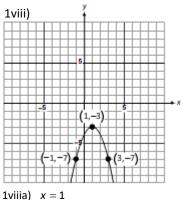
- 2. Write the new equation of the parabola  $y = x^2$  if:
  - a) it undergoes a horizontal translation 2 units to the left and a vertical translation 5 units down and is congruent to  $y = 3x^2$ .
  - b) it undergoes a horizontal translation 2 units right and a vertical translation 3 units up and congruent to  $y = -\frac{1}{2}x^2$ .
  - c) the parabola opens downwards and has been stretched vertically by a factor of 4.
  - d) the parabola opens upwards and has been compressed vertically by a factor of one-third.
  - 3. The path a tennis ball takes from a players forehand ground stroke can be modelled by the function:  $h(d) = -0.015(d-9)^2 + 1.6$ , where h(d) is the height of the ball and d is the horizontal distance the ball has travelled since it was struck.

- a) What is the maximum height the tennis ball reaches?
- b) How far has the ball travelled horizontally from where it was struck when it reaches its maximum height?
- c) What was the height of the ball when it was struck?
- d) How far did the ball travel horizontally from where it was struck to where it landed inside the court?
- e) If the opponent is standing 11 meters away, at what height would he make contact with the ball to volley it back?
- f) State what represents the domain and the range in this example, then list both the domain and the range
- 4. The path a hit baseball takes after leaving a bat can be modelled by the function:  $h(t) = -5.2(t-2.8)^2 + 41.5$ , where h(t) is the height of the ball and t is the elapsed time in seconds since the ball was hit.
  - a) What is the maximum height the baseball reaches?
  - b) What was the height of the baseball when it was struck?
  - c) How long was the ball in the air before it landed on the ground?
  - d) What was the height of the ball after 4 seconds?
  - e) How long was the ball in the air if an outfielder caught the ball one meter off the ground?
  - f) State what represents the domain and the range in this example, then list both the domain and the range
- 5. The path a baseball takes after being hit can be modelled by the function  $h(d) = -0.0095(d-60)^2 + 35$ , where h(d) is the height of the ball and d is the horizontal distance the ball has travelled since it was struck.
  - a) What is the maximum height the baseball reaches?
  - b) How far has the ball travelled horizontally height from where it was struck when it reaches its maximum height?
  - c) Calculate the horizontal distance the ball travelled when it hit the ground?

- d) The ball went over the fence 112 meters away, if the fence was 3 meters tall, by how much did the ball clear the fence?
- e) How far had the ball travelled when it was 20 meters high for the first time?
- f) State what represents the domain and the range in this example, then list both the domain and the range.







<b>1</b> 00000	X 1
1viiib)	down, no compression or expansion
1viiic)	max of $-3$ when x is 1
1viiid)	none (0,-4)
1viiie)	Domain: $x \in R$ Range: $y \leq -3$

2a) 
$$y = 3(x+2)^2 - 5$$
  
2b)  $y = -\frac{1}{2}(x-2)^2 + 3$   
2c)  $y = -4x^2$   
2d)  $y = \frac{1}{3}x^2$ 

- 3a) 1.6 meters
- 3b) 9 meters
- 3c) .385 meters
- 3d) 19.33 meters
- 3e) 1.54 meters
- 3f) Domain: horizontal distance travelled  $0 \le d \le 19.33$ Range: height of the ball  $0 \le h \le 1.6$
- 5a) 35 meters
- 5b) 60 meters
- 5c) 120.7 meters
- 5d) 6.31 meters
- 5e) 20.26 meters
- 5f) Domain: horizontal distance travelled  $0 \le d \le 120.7$ Range: height of the ball  $0 \le h \le 35$

- 4a) 41.5 meters
- 4b) .73 meters
- 4c) 5.63 seconds
- 4d) 34.01 meters
- 4e) 5.59 seconds
- 4f) Domain: elapsed time  $0 \le t \le 5.63$ Range: height of the ball  $0 \le h \le 41.5$