

Math 10

Radicals and Powers

PRACTICE TEST

Name: _____

Learning Goal	Beginning	Developing	Proficient	Sophisticated
I will be able to express a radicals in multiple forms (entire and mixed)				
I will be able to use the laws of exponents to simplify power expressions				

Learning Goal #1: I will be able to express radicals in multiple forms (entire and mixed)

Developing	
Write the below radical as a mixed radical: $\sqrt{45}$ $\begin{array}{r} 5 \overline{)45} \\ \underline{30} \\ 15 \\ \underline{15} \\ 0 \end{array}$ $\sqrt{45} = 3\sqrt{5}$	Write the below radical as a mixed radical: $\sqrt{24}$ $\begin{array}{r} 2 \overline{)24} \\ \underline{4} \\ 0 \end{array}$ $\sqrt{24} = 2\sqrt{6}$
Write the below mixed radical as an entire radical: $2\sqrt{3} = \sqrt{2 \cdot 2 \cdot 3} = \sqrt{12}$	Write the below mixed radical as an entire radical: $3\sqrt{6} = \sqrt{3 \cdot 3 \cdot 6} = \sqrt{54}$

Proficient	
Arrange the mixed radicals from least to greatest: $2\sqrt{3}, 2\sqrt{2}, 2\sqrt{5}, \sqrt{9}, 4\sqrt{3}$ $\sqrt{8} \quad \sqrt{48}$	Write the below radical as a mixed radical: $\sqrt[3]{72m^2n^6}$ $2n^2 \sqrt[3]{9m^2}$

Sophisticated

Arrange the mixed radicals from least to greatest:

$5\sqrt{10}$, $4\sqrt{2}$, $4\sqrt[3]{2}$, $2\sqrt[3]{3}$

$\sqrt{250} \approx 15.8$
 $\sqrt{320} \approx 17.8$
 $\sqrt{128} \approx 11.3$
 $\sqrt[3]{20} \approx 2.7$
 $\sqrt[3]{9} \approx 2.08$
 $\sqrt[3]{27} = 3$

$2\sqrt[3]{3}$, $4\sqrt[3]{2}$, $4\sqrt{2}$, $5\sqrt{10}$, $2\sqrt{5}$, $\sqrt[3]{27}$

Write the below entire radical as a mixed radical:

$\sqrt{108mm^6s^5}$

$\sqrt{108} = 2\sqrt{27} = 2\sqrt{3 \cdot 3 \cdot 3} = 6\sqrt{3}$
 $\sqrt{m^6} = m^3$
 $\sqrt{s^5} = s^2\sqrt{s}$

$6m^3s^2\sqrt{3s}$

Explain (in words) the error in the below solution.

$2\sqrt[3]{3} = 2 * \sqrt[3]{3}$ ← no error.
 $= \sqrt[3]{6} * \sqrt[3]{3}$ ← $2 \neq \sqrt[3]{6} \therefore 2$ would be $\sqrt[3]{8}$
 $= \sqrt[3]{6 * 3}$ ← should be $\sqrt[3]{8 * 3}$
 $= \sqrt[3]{18}$

$\sqrt[3]{24}$

Learning Goal #2: I will be able to use the laws of exponents to simplify power expressions

Developing

Evaluate each power without using a calculator.

$8^{\frac{1}{3}}$ ← p
 $8^{\frac{1}{3}}$ ← r
 $\sqrt[3]{8} = 2$

Evaluate each power without using a calculator.

$36^{0.5} \rightarrow 36^{\frac{1}{2}}$ ← p
 $36^{\frac{1}{2}}$ ← r
 $\sqrt{36} = 6$

Evaluate each power without using a calculator.

$2^{-3} = \frac{1}{2^3} = \frac{1}{8}$

Evaluate each power without using a calculator.

$6^{-2} = \frac{1}{6^2} = \frac{1}{36}$

Proficient

Arrange these numbers in order from least to

greatest: $\sqrt[3]{27}$, $49^{\frac{3}{2}}$, 2^2 , $(\frac{1}{25})^{\frac{3}{2}}$

Handwritten work shows the numbers being converted to a common form for comparison:

- $(\frac{1}{25})^{\frac{3}{2}} = (\frac{1}{5})^3 = \frac{1}{125}$
- $\sqrt[3]{27} = 3$
- $2^2 = 4$
- $49^{\frac{3}{2}} = 343$

The final ordered list is: $(\frac{1}{25})^{\frac{3}{2}}$, $\sqrt[3]{27}$, 2^2 , $49^{\frac{3}{2}}$

Evaluate $16^{1.5}$

Handwritten solution:

$$16^{\frac{3}{2}} = (\sqrt{16})^3 = 4^3 = 64$$

Sophisticated

Simplify

Handwritten simplification of $\sqrt{\frac{x^2}{16y^4}}$:

$$\sqrt{\frac{x^2}{16y^4}} = \frac{\sqrt{x^2}}{\sqrt{16y^4}} = \frac{x}{4y^2}$$

Handwritten simplification of $(\frac{64x^4y^4}{4x^6})^{-\frac{1}{2}}$:

$$\left(\frac{64x^4y^4}{4x^6}\right)^{-\frac{1}{2}} = \left(\frac{16x^4y^4}{x^2}\right)^{-\frac{1}{2}} = \left(\frac{16x^2y^4}{1}\right)^{-\frac{1}{2}} = \frac{1}{\sqrt{16x^2y^4}} = \frac{1}{4xy^2}$$

Evaluate $0.16^{-\frac{3}{2}}$

Handwritten solution:

$$0.16^{-\frac{3}{2}} = \left(\frac{16}{100}\right)^{-\frac{3}{2}} = \left(\frac{100}{16}\right)^{\frac{3}{2}} = \left(\frac{100}{16}\right)^3 = \left(\frac{25}{4}\right)^3 = \frac{15625}{64}$$

Simplify

Handwritten simplification of $(\frac{16x^4y^4}{9x^2y^4})^{-\frac{3}{2}}$:

$$\left(\frac{16x^4y^4}{9x^2y^4}\right)^{-\frac{3}{2}} = \left(\frac{16x^2}{9}\right)^{-\frac{3}{2}} = \left(\frac{9}{16x^2}\right)^{\frac{3}{2}} = \frac{\sqrt{9}}{\sqrt{16x^2}} = \frac{3}{4x}$$

Handwritten simplification of $\left(\frac{(2x^2y^4)(8x^2)}{(3x^2)(3y^4)}\right)^{-\frac{3}{2}}$:

$$\left(\frac{(2x^2y^4)(8x^2)}{(3x^2)(3y^4)}\right)^{-\frac{3}{2}} = \left(\frac{16x^4y^4}{9x^2y^4}\right)^{-\frac{3}{2}} = \left(\frac{16x^2}{9}\right)^{-\frac{3}{2}} = \left(\frac{9}{16x^2}\right)^{\frac{3}{2}} = \frac{\sqrt{9}}{\sqrt{16x^2}} = \frac{3}{4x}$$